

**OPTIMIZING TECHNIQUES**

(Common to CSE and CSS)

Time: 3 hours

Max Marks: 70

Answer any FIVE questions  
All questions carry equal marks

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- 1 (a) What is an inflection point and how do you identify it?  
(b) What is the unimodal property? What is its significance in single variable optimization?
- 2 Given the function:  $f(x_1, x_2) = 100(x_2 - x_1^2) + (1 - x_1)^2$  and  $x^{(0)} = [-1.2, 1]^T$   $x^{(1)} = [-1.3, 1.07]^T$ . The first two points in a search for  $x^*$ , the minimum of  $f$ . calculate the search direction at  $x^{(1)}$  using the Fletcher-Reeves gradient-based method.

Solve the following LP problem using simplex method and comment on the result:

$$\begin{aligned} \text{Maximize } Z &= 2X_1 + 3X_2 \\ -X_1 + 2X_2 &\leq 4 \\ X_1 + X_2 &\leq 6 \\ X_1 + 3X_2 &\leq 9 \\ X_1, X_2 &\geq 0 \end{aligned}$$

- 4 Find the optimal solution for the following transportation problem. The cell entries represent the unit transportation cost in rupees from each factory to each warehouse.

		Warehouse				Supply
		W <sub>1</sub>	W <sub>2</sub>	W <sub>3</sub>	W <sub>4</sub>	
Factory	F <sub>1</sub>	14	25	45	5	6
	F <sub>2</sub>	65	25	35	55	8
	F <sub>3</sub>	35	3	65	15	16
Demand		4	7	6	13	

- 5 Solve the non-linear programming problem:  
optimize  $Z = 4x_1^2 + 2x_2^2 + x_3^2 - 4x_1x_2$   
subject to the constraints  $x_1 + x_2 + x_3 = 15$   
 $2x_1 - x_2 + 2x_3 = 20$ .
- 6 (a) Explain method of multipliers algorithm.  
(b) Describe briefly differences between the MOM and other transformation methods such as SUMT.

Solve the following problem using direct quadratic approximation method:

$$\begin{aligned} \text{Minimize } f(x) &= x_1 x_2 \\ \text{subject to } h(x) &= 6x_1 x_2^{-1} + x_2 x_1^{-2} - 5 = 0 \\ g(x) &= x_1 + x_2 - 1 \geq 0 \\ \text{from the initial feasible estimate } x^0 &= (2, 1). \end{aligned}$$

- 8 (a) Distinguish between PERT and CPM.  
(b) A mother notes that when her teenaged son uses the telephone, he takes no less than 10 minutes for a call and sometimes as much as one hour. Twenty-minute calls are more frequent than calls for any other duration. If son's phone call were an activity in a PERT project:  
(i) What would be the phone call's expected duration?  
(ii) What would be its variance?  
(iii) In scheduling the project, how much time would be allocated for the phone call?

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